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Risk aversion and prudence in contests

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Abstract

I examine the impact of risk preferences on efforts and winning probabilities in generalized Tullock contests between two players. The theoretical analysis yields two main results. First, in symmetric contests, a higher common level of the agents' risk aversion will lead to lower aggregate effort if it comes along with an increase in downside risk aversion. Second, in many asymmetric contests, higher risk-aversion will be a disadvantage if the agent is also more downside risk-averse.

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1. Introduction

Contests are situations in which participants compete for some exogenous rent (prize) by spending non-refundable effort which increases their likelihood of winning. Examples from business, politics, sports, and many other areas of life abound (see e.g. Konrad, 2009). As some element of luck or uncertainty is inherent in contests, the question how individual attitudes towards risk affect the contestants' behaviour suggests itself.

In this paper, I study the influence of individual risk preferences on the equilibrium behaviour in the model of a general two-person Tullock contest under perfect information. The contestants simultaneously choose their effort levels (investments) in order to maximise their expected utility. Describing risk preferences, I focus on *risk aversion* and *prudence (downside risk aversion)*, i.e., on the attitude towards the second (variance) and third moment (skewness) of the relevant lotteries. A risk averse agent is characterised by a negative second derivative of her utility function. As both, downside risk aversion and prudence of an agent, are characterised by a non-negative third derivative of her utility function, the two terms are used synonymously.

First, I compare aggregate efforts across two *symmetric* contests in one of which the common level of risk aversion is higher than in the second. I show that an increase in the common level of risk aversion will reduce aggregate efforts if it comes along with an increase in downside risk aversion as a measure of comparative prudence. This generalises the result that, in a symmetric contest, effort will be lower under risk aversion than under risk neutrality if the risk averse individuals are also downside risk averse or prudent (Treich, 2010).

Second, I analyse individual efforts and odds within an *asymmetric* contest between two agents one of which is more risk averse than the second. For a wide range of parameters, I show that the more risk averse agent will exert less effort and have a smaller chance of winning if she is also more downside risk averse than the second player.

To gain some intuition for these results, notice for a start that the impact of risk aversion on the behaviour in contests is generally ambiguous (see e.g. Konrad and Schlesinger, 1997). Since participation in the contest comes along with an uncertain payment, it may be regarded as a lottery. The general ambiguity then arises because risk aversion induces two opposing effects (see e.g. Skaperdas and Gan, 1995). On the one hand, there is the so called *gambling effect*: The more risk averse the agents are, the fewer lottery tickets they buy since this reduces their safe payment. On the other hand, there is the so called effect of *self-protection*: Buying more lottery tickets, the players can reduce their probability of losing. Therefore, the more risk averse they are, the more they invest. However, a prudent agent is downside risk averse, i.e., the agent prefers some lottery at a higher wealth level over the same lottery at a lower wealth level (Menezes et al., 1980). Thus, as a larger investment lowers the wealth level and increases downside

risk, the gambling effect will dominate the self-protection effect if the agent is comparatively prudent.

The remainder of this paper is organised as follows: In Section 2., I review the related literature. Section 3. introduces the model. In Section 4., I consider symmetric contests, and in Section 5. contests with asymmetric risk preferences. Section 6. concludes.

2. Related Literature

Relatively few papers explicitly address the role of risk preferences in contests. Most of them assume homogeneous players and focus on aggregate effort (rent dissipation). In general, the influence of risk aversion on aggregate effort in symmetric contests with a finite number of players and general contest success functions is ambiguous (Konrad and Schlesinger, 1997). Hillman and Katz (1984) consider a Tullock contest with linear technologies and a large number of homogeneous contestants with a common degree of constant relative risk aversion (CRRA). They show that rent dissipation decreases as the common degree of CRRA increases. Millner and Pratt (1991) present a qualified extension of this result to symmetric Tullock contests with linear technologies and two homogeneous participants: If the agents are risk averse, rent dissipation will be lower than in the case of risk neutral players if and only if the agents are also prudent. Treich (2010) extends the result of Millner and Pratt (1991) to symmetric contests with general contest success functions and any finite number of players showing that aggregate rent seeking efforts of risk averse agents will be lower than in the risk neutral case if the agents are also prudent. As Cornes and Hartley (2012) demonstrate, this result will also hold in asymmetric Tullock contests with linear technologies if no single agent has an equilibrium probability of winning greater than one half. Moreover, they show that in a large symmetric Tullock contest with general technologies rent dissipation is the smaller the higher the common level of risk aversion thereby generalising the original result in Hillman and Katz (1984).

While all these papers examine how changes in common risk preferences influence aggregate behaviour and rent dissipation *across* contests, I also ask how differing risk preferences affect individual behaviour and winning probabilities *within* a given contest. This question has not yet been addressed in the literature for general risk preferences but only for the specific cases of constant absolute risk aversion (CARA, Skaperdas and Gan, 1995, Cornes and Hartley, 2003) and CRRA (Bozhinov, 2006) both of which imply prudence. The authors show that, for such preferences, the less risk averse (and thus less prudent) of any two agents exerts more effort and, therefore, has the better chance of winning.

Hence, the contribution of my paper is twofold. First, I specify a sufficient condition on comparative downside risk aversion under which a higher common level of risk aversion leads to lower aggregate effort in symmetric contests, thereby

generalising the result of Treich (2010). Second, I find that comparative downside risk aversion plays an important role for risk aversion to decrease relative individual effort and thus winning probabilities within a certain contest, thereby extending the analysis of asymmetric risk preferences from the CARA and CRRA cases to general utility functions.

Despite the ambiguous theoretical predictions, most of the experimental studies on the impact of risk preferences in contests find that risk aversion significantly reduces mean individual effort; see e.g. Millner and Pratt (1991), Anderson and Freeborn (2010), or Sheremeta (2011). As there usually is a positive correlation between prudence and risk aversion (Noussair et al., 2014, Ebert and Wiesen, 2014), my theoretical analysis suggests that these results may be driven indirectly by prudence.

3. The Model

Consider a contest between two agents which are identical except for possibly differing risk preferences. Each agent $i \in \{1, 2\}$ has an initial wealth endowment I and can spend some resources $x_i \geq 0$ in order to improve her probability p_i of winning some exogenously given rent $R > 0$. The winning probability is determined by the following contest success function (CSF): If $x_1 = x_2 = 0$ then $p_i := 1/2$, else

$$p_i := \frac{f(x_i)}{f(x_1) + f(x_2)}, \quad (1)$$

where $f : \mathbb{R}_0^+ \rightarrow \mathbb{R}_0^+$ is a twice continuously differentiable function of x_i satisfying $f_i'' \leq 0 < f'$ and $f_i(0) = 0$.

The agents are weakly risk averse. The utility $u_i(z)$ agent $i \in \{1, 2\}$ derives from a certain wealth level z can be expressed by means of some three times continuously differentiable function $u_i : \mathbb{R} \rightarrow \mathbb{R}$ with $u_i'' \leq 0 < u_i'$.

The contest is organised as a simultaneous move game with complete information. The players choose their effort levels x_i in order to maximise their expected utility Eu_i from wealth z_i , which will equal $W_i := I - x_i + R$ if agent i wins the contest and $L_i := I - x_i$ otherwise. Hence, for $i, j \in \{1, 2\}, i \neq j$,

$$\begin{aligned} Eu_i &= p_i u_i(W_i) + (1 - p_i) u_i(L_i) \\ &= \frac{f(x_i)}{f(x_1) + f(x_2)} u_i(I - x_i + R) + \frac{f(x_j)}{f(x_1) + f(x_2)} u_i(I - x_i). \end{aligned}$$

Cornes and Hartley (2012, Theorem 3.1) show that under these assumptions a Nash equilibrium in pure strategies always exists. Moreover, they derive some regularity condition on the curvature of the utility functions u_i under which the Nash equilibrium is unique (Cornes and Hartley, 2012, Theorem 4.2). Yamazaki (2009) shows that, under the assumptions made, the Nash equilibrium in pure strategies will be unique if the Arrow-Pratt measure of absolute risk aversion

$RA(u_i, z) = -\frac{u_i''(z)}{u_i'(z)}$ is non-increasing in the wealth level z for all agents i . All these results hold even for the more general case of a contest between an arbitrary number $n \in \mathbb{N}$ of participants and includes the possibility that some of them might be inactive in equilibrium, i.e., exert zero effort. However, in any equilibrium of a two-player contest, both players will obviously exert positive effort. The corresponding effort levels will hence be fully characterised by the two first order conditions for maximum expected utilities:

$$\frac{\partial p_i}{\partial x_i} = \frac{p_i u_i'(W_i) + (1 - p_i) u_i'(L_i)}{u_i(W_i) - u_i(L_i)}. \quad (2)$$

4. Symmetric Contests

In this section, I suppose that contestants are homogeneous, i.e., $u_i = u$ for $i \in \{1, 2\}$. The contest then has a unique symmetric Nash equilibrium in pure strategies (Cornes and Hartley, 2012, Theorem 4.1). In order to analyse how a change in the common risk preferences influences (aggregate) effort, I compare the symmetric equilibria of two symmetric contests A and B which are identical but with respect to the participants' risk preferences: In contest A , both agents $i \in \{1, 2\}$ have identical preferences described by $u_i = u_A$ and in contest B , both have identical preferences described by $u_i = u_B$.

In general, there is ambiguity whether a rising level of risk aversion *ceteris paribus* decreases the contestant's effort due to the gambling-effect or increases it due to the effect of self-protection (Skaperdas and Gan, 1995, Konrad and Schlesinger, 1997). However, Treich (2010, Proposition 2) shows that if all agents are risk neutral in contest A but risk averse in contest B , efforts will be lower in contest B if the agents in contest B are prudent, i.e., if $u_B''' > 0$.¹ I will generalise this result to the case in which agents are more risk averse in contest B than A with respect to their Arrow-Pratt measure of absolute risk aversion, i.e., $RA(u_B, z) > RA(u_A, z)$ for all possible wealth levels z . In this case, there exists a function $\phi : \mathbb{R} \rightarrow \mathbb{R}$ with $\phi'' < 0 < \phi'$ and $u_B(z) = \phi(u_A(z))$ for all possible wealth levels z , i.e., u_B is a concave transformation of u_A (Mas-Colell et al., 1995, Proposition 6.C.2). If $\phi''' > 0$, Keenan and Snow (2009) define the agents with preferences represented by u_B to be *more downside risk averse* than the agents with preferences represented by u_A and call ϕ a *downside risk averse transformation*. Note that a downside risk averse transformation preserves the prudence property of risk preferences: If $u_B(z) = \phi(u_A(z))$ and $\phi''' > 0$ then $u_B''' \geq 0$ will imply

$$u_B''' = \phi'''(u_A)(u_A')^3 + 3\phi''(u_A)u_A'u_A'' + \phi'(u_A)u_A''' > 0.$$

¹In the case of two players, prudence is even necessary for efforts to be lower (Treich, 2010, Corollary 1).

Proposition 1 *Suppose that contests A and B differ only in the participants' common risk preferences such that agents are more risk averse in contest B , i.e., $u_B = \phi(u_A)$ with $\phi'' < 0 < \phi'$. If the participants in contest B are also more downside risk averse than in contest A , i.e., if $\phi''' > 0$, then efforts will be lower in contest B .*

The proof can be found in the Appendix. Proposition 1 includes the special case of players in contest A being risk neutral as discussed by Treich (2010, Proposition 2) and Cornes and Hartley (2012, Proposition 6.1), respectively.² In this case, $u_A'' \equiv 0 \equiv u_A'''$ and $\phi''' > 0$ then implies $u_B''' > 0$, i.e., the prudence of players in contest B . Note, however, that Proposition 1 will hold even for the players in contest A not being prudent. In this case, the condition $\phi''' > 0$ neither implies the prudence of players in contest B . These considerations show that rather a relative measure of downside risk aversion or prudence than downside risk aversion or prudence per se drives the result.

Keenan and Snow (2009) introduce $S(u, z) := \frac{u'''(z)}{u'_i(z)} - \frac{3}{2} \left(\frac{u''(z)}{u'_i(z)} \right)^2$ as a local index of downside risk aversion and show that the condition $S(u_B, z) \geq S(u_A, z)$ for all possible z is sufficient for the existence of a transformation ϕ with $u_B = \phi(u_A)$ and $\phi''' > 0$. Thus, Proposition 1 also holds if the condition $\phi''' > 0$ is replaced by the (possibly stronger) condition $S(u_B, z) \geq S(u_A, z)$ for all possible z . Similarly, Keenan and Snow (2010) formulate sufficient conditions under which an increase in downside risk aversion is implied by appropriate uniform changes in two alternative local measures, the coefficient of absolute prudence $PA(u, z) := -\frac{u'''(z)}{u''(z)}$ introduced by Kimball (1990) and the alternative measure of downside risk aversion $D(u, z) := \frac{u'''(z)}{u'(z)}$ proposed by Modica and Scarsini (2005) and Crainich and Eeckhoudt (2008), respectively.

5. Contests with Asymmetric Risk Preferences

In order to analyse how differences in the agents' risk preferences influence individual efforts and odds within a certain contest, I assume agent 1 to be more risk averse than agent 2 with respect to the Arrow-Pratt measure of absolute risk aversion, i.e., $RA(u_1, z) > RA(u_2, z)$ for all possible wealth levels z . As above, there exists a function $\phi: \mathbb{R} \rightarrow \mathbb{R}$ with $\phi'' < 0 < \phi'$ and $u_1(z) = \phi(u_2(z))$ for all possible wealth levels z , i.e., u_1 is a concave transformation of u_2 .

If players exhibit CARA, the less risk averse will exert higher effort and therefore have a better chance of winning (Skaperdas and Gan, 1995, Cornes and Hart-

²For contests with an arbitrary number n of participants, Cornes and Hartley (2012, Corollary 6.1) show that the effort of the more risk averse players in contest B will be smaller than the effort of the less risk averse players in contest A if n is sufficiently large. Under the additional condition that u_B is a downside risk averse transformation of u_A , Proposition 1 extends their finding to the case of $n = 2$.

ley, 2003). The following example shows, however, that this result does not hold in general.³

Example 1 *Assume $u_1(z) = -(1-z)^2$, $u_2(z) = z$, $f(x) = x$, and $I+R < 1$, i.e., a lottery contest between some risk averse agent 1 and some risk neutral agent 2. Straightforward calculations show that the game has a Nash equilibrium in pure strategies in which both agents choose the same effort level $x_1 = x_2 = R/4$ and, hence, have the same winning probability $p_1 = p_2 = 1/2$.*

The example is instructive in explaining why an agent's risk aversion alone will not necessarily induce a behaviour that is different from the one of a risk neutral opponent. While the latter only cares about the mean of the lottery associated with the contest, quadratic risk preferences imply that the former only cares about the mean and variance which equals $p(1-p)R^2$. Hence, for $p = 1/2$ a marginal change in the winning probability induced by a marginal investment in effort has no effect on the variance of the lottery, i.e., the marginal calculus is identical for both agents.

The crucial difference between this example and the CARA-case is the fact that CARA-preferences imply that the respective agent is not only risk averse but also prudent. Prudent agents are downside risk averse and, therefore, prefer some lottery at a higher wealth level over the same lottery at a lower wealth level. Hence, even in a situation like in the example above in which the marginal investment has no impact on the variance, a prudent contestant has, *ceteris paribus*, an incentive to invest less than a risk neutral agent in order to increase the wealth level $I - x$ at which the lottery takes place.

These considerations provide some intuition for why the comparative level of prudence or downside risk aversion plays an important role for the agents' relative efforts. The following Lemma states that, unlike in the example above, the asymmetric contest will never have a symmetric equilibrium if u_1 is a downside risk averse transformation of u_2 .

Lemma 1 *Suppose that the contestants differ only in their risk preferences such that agent 1 is more risk averse than agent 2, i.e., $u_1 = \phi(u_2)$ with $\phi'' < 0 < \phi'$. If agent 1 is also more downside risk averse than agent 2, i.e., if $\phi''' > 0$, then equilibrium efforts and odds will differ, i.e., $x_1 \neq x_2$ and $p_1 \neq p_2$.*

The proof can be found in the Appendix. Proposition 1 and the CARA-case suggest that the more risk averse agent will exert less effort and have a smaller chance of winning if she is also more downside risk averse, i.e., if her preferences are a downside risk averse transformation of the second player's preferences. The proof that this conjecture holds for a wide range of parameters

³In a model of optimal prevention, Eeckhoudt and Gollier (2005, Proposition 1) find that, when the optimal probability of loss of the risk neutral agent is $1/2$, adding risk aversion but not prudence has no effect on the optimal level of effort. The example illustrates that this result may hold even in (asymmetric) situations of strategic interaction.

(R, I, f, u, ϕ) specifying the contest is based on the following idea. Start from a contest $(R_0, I_0, f_0, u_0, \phi_0)$ for which the parameters satisfy the conditions of Lemma 1 and the more risk averse agent indeed exerts less effort in equilibrium, i.e., $x_1(R_0, I_0, f_0, u_0, \phi_0) < x_2(R_0, I_0, f_0, u_0, \phi_0)$, like e.g. for some case with CARA-preferences. Then, any continuous change to the parameters (R, I, f, u, ϕ) within the class satisfying the conditions of Lemma 1, which leads to some continuous shift of the equilibrium, preserves $x_1(R, I, f, u, \phi) < x_2(R, I, f, u, \phi)$ by Lemma 1 and the intermediate value theorem.

Formalising this idea in Proposition 2 requires some further notation. Denote by $\mathbb{C}^k(X)$ the set of all k -times continuously differentiable real functions on some compact $X \subset \mathbb{R}_0^+$ and define

$$\begin{aligned} A &:= \{f \in \mathbb{C}^2(X) \mid f(0) = 0, f'(x) > 0 \geq f''(x) \text{ for all } x \in X\}, \\ B &:= \{u \in \mathbb{C}^3(X) \mid u'(x) > 0 \geq u''(x) \text{ for all } x \in X\}, \\ C &:= \{\phi \in \mathbb{C}^3(X) \mid \phi'(x) > 0 > \phi''(x), \phi'''(x) > 0 \text{ for all } x \in X\}. \end{aligned}$$

Note that $X, A, B,$ and C are connected topological spaces and so is the product space $P = X \times X \times A \times B \times C$. Let M be a connected subset of P for which the contest has a unique equilibrium in pure strategies.⁴ For each element of M , denote this equilibrium by $(x_1^*(R, I, f, u, \phi), x_2^*(R, I, f, u, \phi))$.

Proposition 2 *Let S be a connected subset of M on which*

$$\Delta x(R, I, f, u, \phi) := x_2^*(R, I, f, u, \phi) - x_1^*(R, I, f, u, \phi)$$

*is continuous.*⁵ *If there is some $(R_0, I_0, f_0, u_0, \phi_0) \in S$ with $\Delta x(R_0, I_0, f_0, u_0, \phi_0) > 0$, then $\Delta x(R, I, f, u, \phi) > 0$ for all $(R, I, f, u, \phi) \in S$.*

Proof. Suppose to the contrary that there is some $(R, I, f, u, \phi) \in S$ such that $\Delta x(R, I, f, u, \phi) \leq 0$. The intermediate value theorem then implies the existence of some $(\hat{R}, \hat{I}, \hat{f}, \hat{u}, \hat{\phi}) \in S$ such that $\Delta x(\hat{R}, \hat{I}, \hat{f}, \hat{u}, \hat{\phi}) = 0$, a contradiction to Lemma 1.⁶

□

6. Concluding Remarks

In this paper, I have examined the impact of risk preferences on efforts and winning probabilities in generalised Tullock contests between two players. In symmetric contests, an increase in the common level of the agents' risk aversion leads

⁴Yamazaki (2009) as well as Cornes and Hartley (2012, Theorem 4.2) provide sufficient conditions for equilibria in pure strategies to be unique.

⁵Generalizations of the implicit function theorem (Krantz and Parks, 2013) guarantee the existence of such a subset S .

⁶Similar applications of the intermediate value theorem have been used to prove the existence of general equilibria (see, e.g., John, 1999) or fixed points (see, e.g., Mas-Colell et al., 1995, page 952).

to lower aggregate effort if it comes along with increasing downside risk aversion. Moreover, I have shown that in asymmetric contests, higher risk-aversion will be a disadvantage for an abstract range of parameters if the agent is also more downside risk averse. Future work may further specify this range of parameters by characterising the (maximum) subset S on which Proposition 2 applies.

Lemma 1 implies that the effort levels or winning probabilities of two agents, one of which is more risk averse and downside risk averse, may coincide only if they differ also in some other characteristic besides risk preferences. Put differently, whenever Proposition 2 applies, keeping up with the less risk averse requires, *ceteris paribus*, an advantage in a second dimension, e.g., higher ability (March and Sahn, 2017).

Appendix: Proofs

Proof of Proposition 1.

Remember that the symmetric contest $C \in \{A, B\}$ has a unique symmetric equilibrium (x_C, x_C) satisfying condition (2). Define

$$p_x := \frac{\partial p_i(x, x)}{\partial x_i} = \frac{1}{4} \frac{f'(x)}{f(x)}$$

for $i \in \{1, 2\}$ and

$$F_C(x) := p_x[u_C(W) - u_C(L)] - \frac{1}{2}[u'_C(W) + u'_C(L)]$$

for all $x > 0$. By definition, F_C is continuous in x , has a unique zero at x_C , and satisfies $\lim_{x \rightarrow 0} F_C(x) > 0$ as well as $\lim_{x \rightarrow \infty} F_C(x) < 0$ due to the properties of f . The intermediate value theorem then implies that $F_C(x) > 0$ if and only if $x < x_C$. In particular, $x_B < x_A \Leftrightarrow F_A(x_B) > 0$. In what follows, I will show the validity of the latter inequality.

With $u_B = \phi(u_A)$, the identity $F_B(x_B) = 0$ implies

$$p_{x_B} = \frac{1}{2} \frac{\phi'(u_A(W_B))u'_A(W_B) + \phi'(u_A(L_B))u'_A(L_B)}{\phi(u_A(W_B)) - \phi(u_A(L_B))}.$$

Using this equation, $F_A(x_B) > 0$ is equivalent to

$$\frac{[\phi'(u(W))u'(W) + \phi'(u(L))u'(L)][u(W) - u(L)]}{[\phi(u(W)) - \phi(u(L))][u'(W) + u'(L)]} > 1 \quad (3)$$

with $u = u_A$, $W = W_B = I - x_B + R$, and $L = L_B = I - x_B$. To show the validity of inequality (3), first note that

$$\frac{\phi'(u(W))u'(W) + \phi'(u(L))u'(L)}{u'(W) + u'(L)} \geq \frac{1}{2}[\phi'(u(W)) + \phi'(u(L))]$$

$$\Leftrightarrow [\phi'(u(W)) - \phi'(u(L))][u'(W) - u'(L)] \geq 0,$$

which is true due to the concavity of ϕ and u since u is increasing and $W > L$. Hence, it is sufficient to show that

$$\begin{aligned} & \frac{1}{2}[\phi'(u(W)) + \phi'(u(L))]\frac{u(W) - u(L)}{\phi(u(W)) - \phi(u(L))} > 1 \\ \Leftrightarrow & \frac{1}{2}[\phi'(u(W)) + \phi'(u(L))] - \frac{\phi(u(W)) - \phi(u(L))}{u(W) - u(L)} > 0. \end{aligned}$$

However, this last inequality follows from Eeckhoudt and Gollier (2005, Lemma 1) and the strict convexity of ϕ' . □

Proof of Lemma 1.

The proof is by contradiction. I write $u_2 = u$ and $u_1 = \phi(u)$ as well as $W_i = I - x_i + R$ and $L_i = I - x_i$ for short. Note that

$$\frac{\partial p_i}{\partial x_i} = \frac{f'(x_i)f(x_j)}{[f(x_i) + f(x_j)]^2}$$

for $i, j \in \{1, 2\}$ with $i \neq j$. Dividing the first order condition (2) for agent 1 by the one for agent 2 yields

$$\frac{f'(x_1)f(x_2)}{f'(x_2)f(x_1)} = \frac{[p_1\phi'(u(W_1))u'(W_1) + p_2\phi'(u(L_1))u'(L_1)][u(W_2) - u(L_2)]}{[\phi(u(W_1)) - \phi(u(L_1))][p_2u'(W_2) + p_1u'(L_2)]} \quad (4)$$

Now suppose that there is an equilibrium with $x_1 = x_2 = x$ and, hence, $W_1 = W_2 = W$, $L_1 = L_2 = L$, as well as $p_1 = p_2 = 1/2$. Then, obviously the left hand side of equation (4) equals 1. However, the right hand side of equation (4) is equal to the term on the left hand side of inequality (3) and, hence, larger than 1 as show in the proof of Proposition 1. □

References

- Anderson, L. R. and B. A. Freeborn (2010) “Varying the intensity of competition in a multiple prize rent seeking experiment” *Public Choice* **143**(1-2), 237–254.
- Bozhinov, P. (2006) *Constant relative risk aversion and rent-seeking games*, PhD thesis: Keele University.
- Cornes, R. and R. Hartley (2012) “Risk aversion in symmetric and asymmetric contests” *Economic Theory* **51**(2), 247–275.

- Cornes, R. and R. Hartley (2003) “Risk aversion, heterogeneity and contests” *Public Choice* **117**, 1–25.
- Crainich, D. and L. Eeckhoudt (2008) “On the intensity of downside risk aversion” *Journal of Risk and Uncertainty* **36**(3), 267–276.
- Ebert, S. and D. Wiesen (2014) “Joint measurement of risk aversion, prudence, and temperance” *Journal of Risk and Uncertainty* **48**(3), 231–252.
- Eeckhoudt, L. and C. Gollier (2005) “The impact of prudence on optimal prevention” *Economic Theory* **26**(4), 989–994.
- Hillman, A. L. and E. Katz (1984) “Risk-averse rent seekers and the social cost of monopoly power” *The Economic Journal* **94**, 104–110.
- John, R. (1999) “Abraham wald’s equilibrium existence proof reconsidered” *Economic Theory* **13**(2), 417–428.
- Keenan, D. C. and A. Snow (2010) “Greater prudence and greater downside risk aversion” *Journal of Economic Theory* **145**(5), 2018 – 2026.
- Keenan, D. C. and A. Snow (2009) “Greater downside risk aversion in the large” *Journal of Economic Theory* **144**(3), 1092 – 1101.
- Kimball, M. S. (1990) “Precautionary saving in the small and in the large” *Econometrica* **58**(1), 53–73.
- Konrad, K. A. (2009) *Strategy and Dynamics in Contests*, Oxford University Press: New York.
- Konrad, K. and H. Schlesinger (1997) “Risk aversion in rent-seeking and rent-augmenting games” *The Economic Journal* **107**, 1671–1683.
- Krantz, S. G. and H. R. Parks (2013) *The Implicit Function Theorem*, Birkhäuser: Basel.
- March, C. and M. Sahm (2017) “Contests as selection mechanisms: The impact of risk aversion” Mimeo: University of Bamberg.
- Mas-Colell, A., M. Whinston, and J. Green (1995) *Microeconomic Theory*, Oxford University Press: New York.
- Menezes, C., C. Geiss, and J. Tressler (1980) “Increasing downside risk” *American Economic Review* **70**(5), 921–932.
- Millner, E. L. and M. D. Pratt, (1991) “Risk aversion and rent-seeking: An extension and some experimental evidence” *Public Choice* **69**(1), 81–92.

- Modica, S. and M. Scarsini (2005) “A note on comparative downside risk aversion” *Journal of Economic Theory* **122**(2), 267 – 271.
- Noussair, C. N., S. T. Trautmann, and G. van de Kuilen (2014) “Higher order risk attitudes, demographics, and financial decisions” *The Review of Economic Studies* **81**(1), 325-355.
- Sheremeta, R. M. (2011). “Contest design: An experimental investigation” *Economic Inquiry* **49**(2), 573–590.
- Skaperdas, S. and L. Gan (1995) “Risk aversion in contests” *The Economic Journal* **105**, 951–962.
- Treich, N. (2010) “Risk-aversion and prudence in rent-seeking games” *Public Choice* **145**(3-4), 339–349.
- Yamazaki, T. (2009) “The uniqueness of pure-strategy Nash equilibrium in rent-seeking games with risk-averse players” *Public Choice* **139**(3-4), 335–342.